

Cryptography:

Information **confidentiality**, **integrity**,
authenticity, **person identification**

Symmetric cryptography ----- Asymmetric cryptography

Symmetric encryption

H-functions, Message digest
HMAC H-Message Authentication
Code

$$P(1 \text{ move}) = 1/2$$

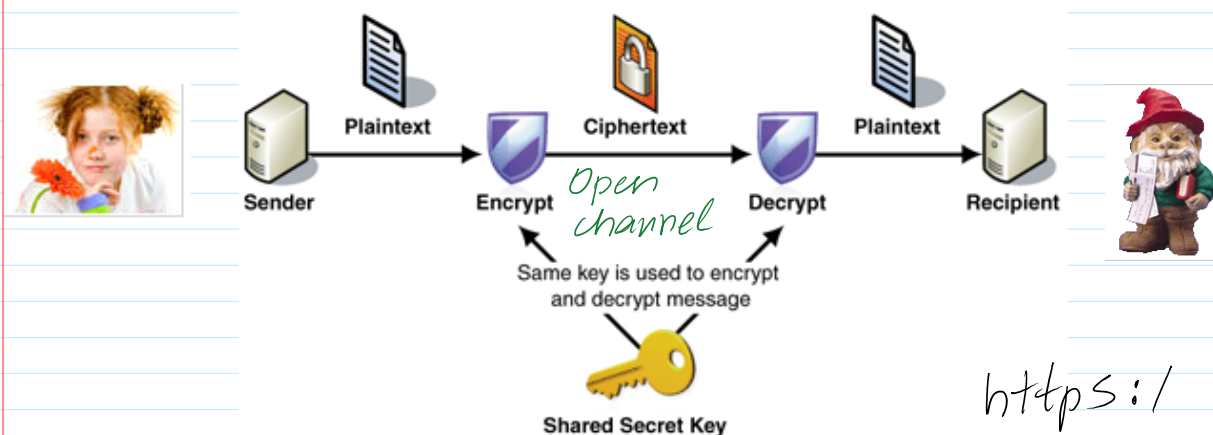
$$10 \text{ moves} \rightarrow 2^{10} = 1024$$

$$P(10 \text{ moves}) = 1/1024$$

Asymmetric encryption

E-signature - Public Key Infrastructure - PKI
Data authenticity
Person identification
E-money
E-voting
Digital Rights Management - DRM
Etc.

Symmetric encryption



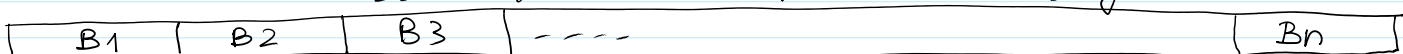
<https://k4p>

AES - 128, 192, 256 Block cipher --> Encryption --> Decryption

Advanced Encryption Standard ~ 2000

Key length 128, 192, 256 bits: $k \in \{128 \text{ b}, 192 \text{ b}, 256 \text{ b}\}$

Data to be encrypted: message m



The length of any block B_i should be $|B_i| = 128 \text{ bits}$
192 bits

The length of any block B_i should be $|B_i| = 128 \text{ bits}$
 $|B_i| = |k|$
 192 bits
 256 bits

$$\text{EncAES}(k, B_1) = C_1$$

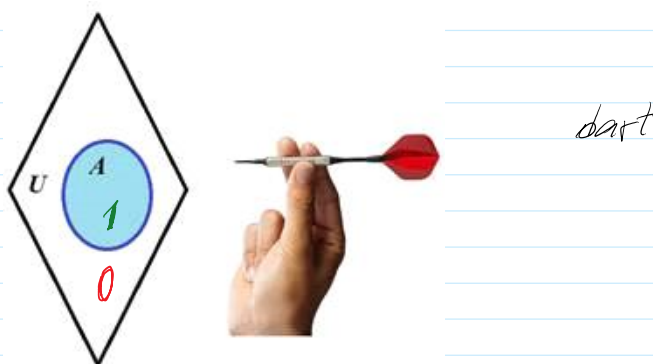
$$\text{EncAES}(k, B_2) = C_2$$

$$\text{EncAES}(k, B_n) = C_n$$

$$\text{EncAES}(k, m) = c \xrightarrow{c} \text{DecAES}(k, c) = m$$

Vernam cipher (1917) - One Time Pad

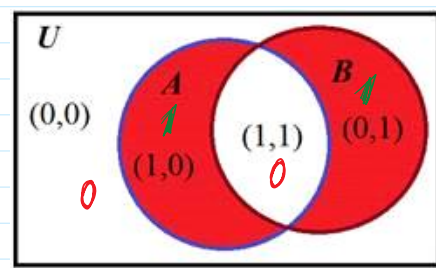
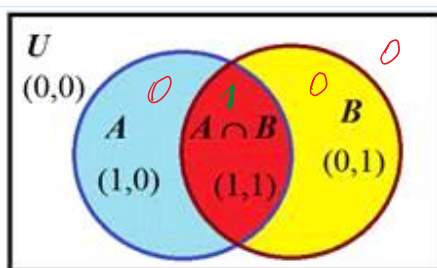
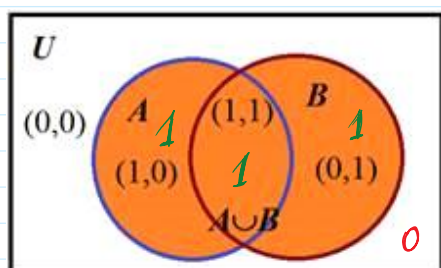
Logical operations



$A \cup B$

$A \cap B$

$A \oplus B$



"0" No

"1" Yes

$$m \in \{0, 1\}$$

$$k \leftarrow \text{rand}(\{0, 1\}) ; k \in \{0, 1\}$$

$$c = m \oplus k$$

$$\Pr(k=0) = 1/2$$

$$\Pr(k=1) = 1/2$$

c
 if $c=0$
 if $c=1$ } eavesdropping adversary

A	B	$A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

m	k	$m \oplus k = c$
0	0	0
0	1	1
1	0	1
1	1	0

\oplus - is inverse to itself

$$c - k = m$$

$$c = m \oplus \cancel{k} - \cancel{k} = m$$

$$c = m \oplus \cancel{k} \oplus \cancel{k} =$$

$$= m \oplus 0 = m = 1$$

Alice: $k = 1$.

Let $m = 1$; $k = 1$: $\Pr(k=1) = 1/2$

$$c = m \oplus k = 1 \oplus 1 = 0$$

$$c = 0$$

Bob: $k = 1$.

$$c \oplus k = 0 \oplus 1 = 1 = m.$$

But nevertheless, the reader confusing implication and equivalence operations (functions) can accept the following proposition as valid:

if talker has a head and donkey has a head, then talker is a donkey.

To accept this proposition as valid means that thinker confuses notions of implication and equivalence. If reader is afraid to make such a mistake, we recommend to read about that in any external source.

```
>> m=77000
```

```
m = 77000
```

```
>> mb=dec2bin(m)
```

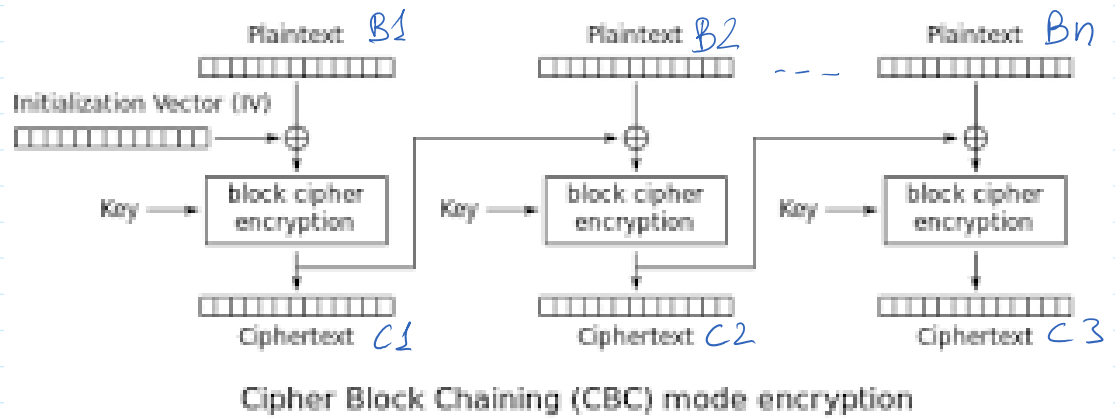
```
mb = 10010110011001000
```

message m consist of 17 bits: $|m| = 17$ bits.

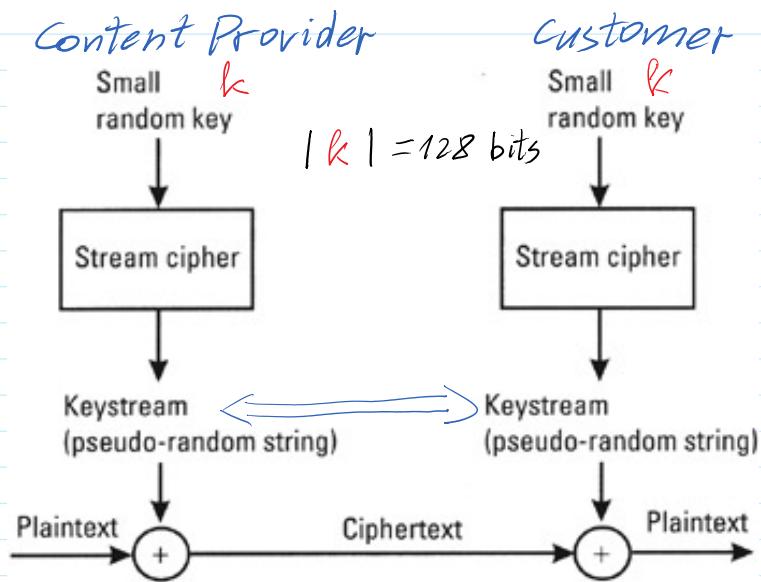
Symmetric encryption

- **block cipher** is one in which a block of plaintext is treated as a whole and used to produce a cipher text block of equal length.

in which message (plain text) of any finite length is divided into the number of same length block and every block is encrypted with the same relatively short key of length 128 bits, 192 bits, 256 bits or the similar length



AES-128-CBC : $|B_1| = |B_2| = \dots = |B_n| = 128 \text{ bits}$



- A **stream cipher** is one that encrypts a digital data stream one bit or one byte at a time. Examples of classical stream ciphers are the auto keyed Vigenère cipher and the Vernam cipher.